

A Speculative Model of Coupled Mirror Universes

Algebraic Structure, Recursive Compression, and a Documented Human–AI Collaborative Process

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In collaboration with ChatGPT (OpenAI), Grok (xAI), and Claude (Anthropic)

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Editorial note (consolidated edition). This document consolidates several overlapping versions of a personal research archive (a core manuscript, an appendix of process transcripts, and supporting captures) into a single coherent text. Redundant material has been removed and the strongest explanation of each concept retained. The work is explicitly *speculative*: it is offered as a well-formulated question, not as a validated physical theory. Following the author’s own method, the manuscript maintains four visible epistemic layers — **rigorous**, **empirical**, **speculative**, and **poetic** — and never presents speculation as established fact.

Keywords: mirror universes · cosmological constant · quaternions · octonions · emergent time · recursive compression · human–AI collaboration · speculative cosmology · distributed cognition

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1. Executive Summary

This manuscript proposes a speculative cosmological framework in which the observable universe (**A**) is globally coupled to a complementary mirror universe (**B**) through a non-local, antisymmetric geometric interaction. Within this picture, the observed accelerated expansion — conventionally attributed to the cosmological constant Λ — is reinterpreted as an *emergent geometric effect* of the coupling rather than as a distinct substance with negative pressure. The Friedmann equations are left structurally unmodified; Λ is read as a parameter encoding membership in a larger symmetric structure.

The framework's central analytical claim is algebraic: the antisymmetric A–B dynamics share the formal structure of quaternionic non-commutativity (universe A $\leftrightarrow i$, universe B $\leftrightarrow j$, the inter-universe coupling $\leftrightarrow$ the emergent element $k = ij = -ji$). A deeper, path-dependent projective structure — if it holds — would force a non-associative algebra, i.e. the octonions ($\mathbb{O}$), with $G_2 = \text{Aut}(\mathbb{O})$ as a candidate symmetry of the membrane.

A second, methodological contribution is the explicit documentation of the *process* by which the model was developed: roughly seven months of recursive compression and iteration across multiple AI systems, in two languages, under widely varying cognitive states. The author argues that this distributed, constraint-driven process is itself part of the result and reports it transparently, including what was deliberately discarded.

2. Abstract

We present a speculative cosmological framework in which the observable universe (A) is globally coupled to a complementary mirror universe (B) through a non-local geometric interaction. The accelerated expansion attributed in standard cosmology to the cosmological constant Λ is proposed to be an emergent geometric effect of an antisymmetric global coupling, requiring no exotic substance; the Friedmann equations remain unmodified and Λ is reinterpreted as a parameter encoding membership in a larger symmetric cosmological structure. A central contribution is the identification of the model's natural algebraic home: the antisymmetric A–B dynamics correspond to the non-commutativity of the quaternions ($\mathbb{H}$), with A $\leftrightarrow i$, B $\leftrightarrow j$, and the coupling membrane as the emergent element $k = ij = -ji$. The mathematical hierarchy $\mathbb{N} \subset \mathbb{R} \subset \mathbb{C} \subset \mathbb{H} \subset \mathbb{O}$ is placed in correspondence with the physical structure: discrete pre-Big-Bang states ($\mathbb{N}$), emergent spacetime ($\mathbb{R}$), global entropy balance as phase conservation ($\mathbb{C}$), observable antisymmetric dynamics ($\mathbb{H}$), and a speculative deep projective structure ($\mathbb{O}$). The Big Bang is interpreted as the $\mathbb{N} \rightarrow \mathbb{R}$ transition, the point at which discrete degrees of freedom give way to a continuous manifold in which time becomes possible. By Hurwitz's theorem, if the projective composition of the deep structure is path-dependent, the octonions are the only available division algebra and $G_2 = \text{Aut}(\mathbb{O})$ becomes a candidate membrane symmetry. The manuscript documents its four-layer epistemic structure (rigorous, empirical, speculative, poetic) and treats the human–AI collaborative process — seven months of iterative development across ChatGPT, Grok, and Claude — as part of the reported result.

3. Introduction

The standard cosmological model (Λ CDM) accounts for the observed accelerated expansion of the universe by introducing a cosmological constant Λ , often interpreted as a vacuum energy density with negative pressure. While empirically successful, this interpretation leaves the physical origin and the magnitude of Λ unexplained. This manuscript explores an alternative *interpretive* framing: that the effect encoded by Λ may be a geometric signature of belonging to a larger, symmetric structure rather than evidence of a new substance.

The proposal is deliberately modest in its empirical commitments. It does *not* modify the Friedmann equations, predict new local phenomena, or claim observational superiority over Λ CDM in the present regime. Instead, it asks whether a coupled two-universe geometry can reproduce the same phenomenology while offering a different account of *why* the dark-energy term takes the form it does. In this sense the contribution is a reframing and an algebraic organization of an existing observation, not a new empirical prediction.

Two threads run through the work. The first is physical and mathematical: the construction of the mirror coupling and the identification of its natural algebraic setting. The second is methodological and reflective: a transparent account of how the framework was produced through a long, recursive human–AI collaboration. The author’s stated position — preserved here — is that keeping the boundaries between rigorous, empirical, speculative, and poetic content visible is a scientific virtue, because it allows a future reader to know exactly what was established, what was hypothesized, and what was metaphor.

4. Background

4.1 Standard cosmology and the cosmological constant

In the Friedmann–Lemaître framework, the expansion of a homogeneous, isotropic universe is governed by the Friedmann equation, here written schematically as:

$$(\dot{a}/a)^2 = (8\pi G/3)\rho - k/a^2 + \Lambda/3$$

where a is the scale factor, ρ the energy density, k the spatial curvature, and Λ the cosmological constant. In Λ CDM, Λ is treated as an independent constant associated with vacuum energy. The present framework retains this equation unchanged but reinterprets the role of Λ .

4.2 Normed division algebras

The real numbers ($\mathbb{R}$), complex numbers ($\mathbb{C}$), quaternions ($\mathbb{H}$), and octonions ($\mathbb{O}$) form the complete set of normed division algebras over the reals, a result established by Hurwitz’s theorem (1898). Ascending the chain $\mathbb{R} \subset \mathbb{C} \subset \mathbb{H} \subset \mathbb{O}$, each extension doubles the dimension and surrenders a structural property: $\mathbb{C}$ loses the natural ordering of $\mathbb{R}$; $\mathbb{H}$ loses commutativity; $\mathbb{O}$ loses associativity. The quaternions encode three-dimensional rotations through their non-commutative product ($ij = k, ji = -k$); the octonions are the unique non-associative normed division algebra, and their automorphism group is the exceptional Lie group G_2 . These are standard mathematical facts; the framework’s novelty lies in the proposed *correspondence* between this hierarchy and a cosmological structure, not in the mathematics itself.

4.3 Prior internal development

This manuscript is the consolidation of an evolving personal archive (informally versioned v1–v15, October 2025 – May 2026; see §9.3). Earlier versions developed the coupled-universe dynamics, entropy and arrow-of-time arguments, and a series of appendices; later versions introduced the algebraic compression that is foregrounded here. The consolidated edition retains the surviving claims and discards material identified by the author as method-mistaken-for-result or metaphor-mistaken-for-physics (see §7.3).

5. Methodology

Because this is a conceptual and analytical work rather than an experimental one, the “Methodology” describes the *analytical and editorial procedures* used to develop and compress the framework. No physical experiment or numerical simulation is claimed.

5.1 The model construction

The physical model is specified by a small set of postulates (§6.1) from which the antisymmetric dynamics and the Λ reinterpretation follow. The construction is deductive: given the postulates, the behaviour of the coupled system and its algebraic signature are derived rather than fitted to data.

5.2 Recursive compression

The principal analytical method is *recursive compression*: the full archive (estimated at ~500,000 words across v1–v15 and supplementary material) was repeatedly distilled, each pass discarding restatement and metaphor while retaining only claims that survived re-examination. The author reports that the technical constraints of the AI systems used — finite context windows and the absence of cross-session memory — *forced* this compression at each step, and argues that the constraint was generative rather than obstructive (§9.5).

5.3 Palindromic / mirror iteration

A complementary procedure, described in the archive as the “palindromic mirror” method, ran ideas forward and then in reverse (an expansion $1 \rightarrow 2 \rightarrow 3 \rightarrow 4$ followed by a contraction $4 \rightarrow 3 \rightarrow 2 \rightarrow 1$), using the reverse pass as a filter. The author is explicit that this is a *method*, not a result, and the consolidated edition treats it accordingly.

5.4 Multi-system human–AI iteration

Development proceeded as a dialogue across three AI systems with distinct roles (ChatGPT as critical editor and structural clarifier; Grok as high-entropy interlocutor and algebraic explorer; Claude as final distiller and synthesizer), with the human author retaining all creative direction and all decisions about what to keep or discard (§9). A notable feature of the process was the use of high-entropy, compressed keyboard input during high-cognitive-load states, which the AI systems treated as signal to be decoded into the nearest coherent intent — an interaction style the author documents as part of the method.

6. The Model and Its Analyses

This section corresponds to what an empirical paper would call “Experiments.” Here it sets out the model and the analytical derivations (the “bridges”) that were tested for internal consistency. The outcomes of these analyses are reported in §7.

6.1 Basic postulates

1. Two mirror universes A and B exist and are globally symmetric.
2. Each universe is individually homogeneous and isotropic at large scales.
3. There is no local interaction or direct causal exchange between A and B.
4. The coupling is global, geometric, and effective — not a classical force.
5. The total system preserves global symmetry throughout its evolution.

6.2 Antisymmetric dynamics

The A–B system evolves through antisymmetric alternation: when A undergoes accelerated expansion, B undergoes accelerated contraction. This is presented not as a classical force but as an emergent geometric response of the coupled system. The symbolic geometric identity is:

$$G_A(a, \rho, P, k_{\text{eff}}) = G_B(a, \rho, -P, k_{\text{eff}})$$

The pressure inversion ($P \rightarrow -P$) reflects the antisymmetric character. The Friedmann equation (§4.1) is retained unchanged; Λ is reinterpreted as the effective parameter encoding the global geometric coupling rather than an independent substance.

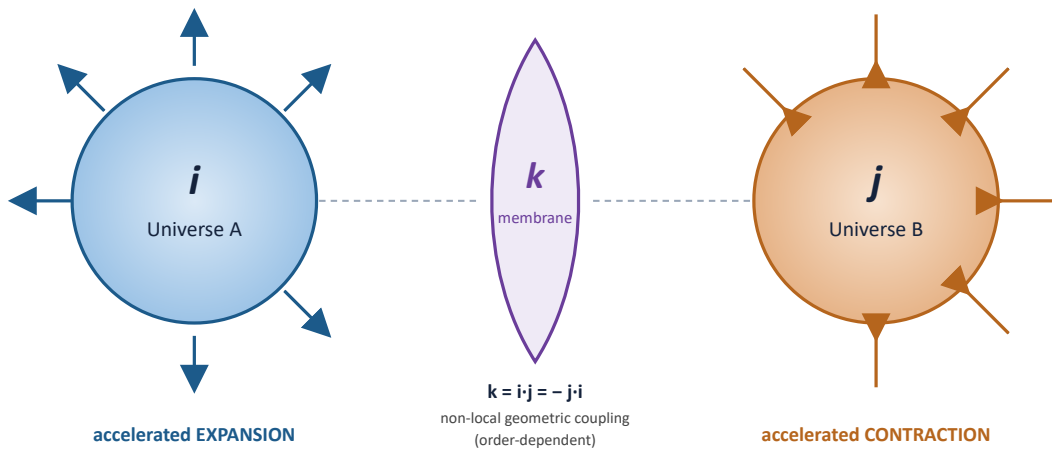


Figure 1. Antisymmetric A–B coupling. When A expands, B contracts; the emergent, order-dependent coupling element k is the quaternionic imaginary unit $i \cdot j = -j \cdot i$ (§6.2, §6.5).

6.3 Entropy, phase conservation, and emergent time

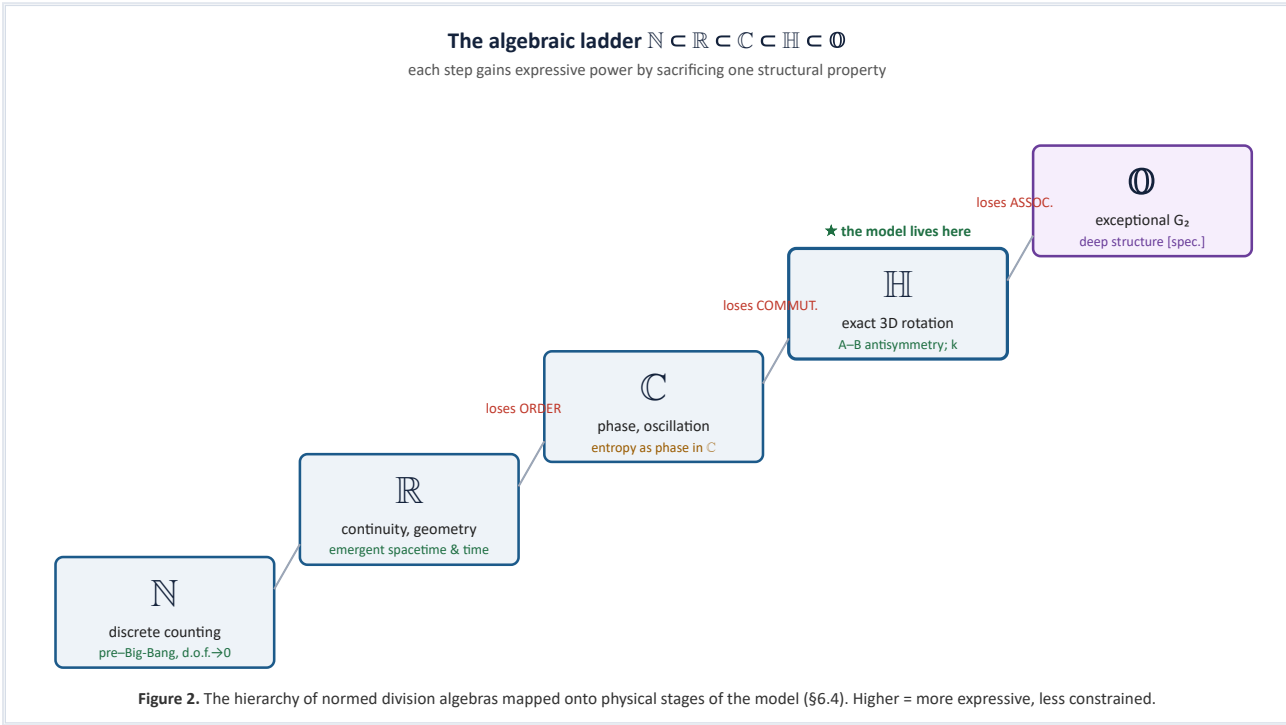
Global entropy is taken to be conserved, $S_A + S_B \approx \text{const}$. This is placed in structural correspondence with norm conservation in $\mathbb{C}$: setting $S_A = \cos^2\theta$ and $S_B = \sin^2\theta$ satisfies $\cos^2\theta + \sin^2\theta = 1$ identically, so the cosmological cycle is parameterized as a phase rotation $\theta(t)$ in the complex plane. The Wick rotation $t \rightarrow -i\tau$ connects the temporal oscillation to a statistical (Euclidean) distribution of entropy. Time is

treated as *emergent*: it does not exist “before” the Big Bang because the $\mathbb{R}$ -continuum that makes “between two instants” meaningful does not yet exist. The Big Bang is the $\mathbb{N} \rightarrow \mathbb{R}$ transition.

6.4 The algebraic map $\mathbb{N} \subset \mathbb{R} \subset \mathbb{C} \subset \mathbb{H} \subset \mathbb{O}$

Each algebraic extension trades a structural property for expressive capacity; the framework maps this hierarchy onto the physical structure of the model.

Algebra	Dim	Ordered	Commut.	Assoc.	Gains	Role in the A–B model
$\mathbb{N}$	1	yes	yes	yes	discrete counting	pre–Big–Bang state, d.o.f. $\rightarrow 0$
$\mathbb{R}$	1	yes	yes	yes	continuity, geometry	emergent spacetime and time
$\mathbb{C}$	2	no	yes	yes	phase, oscillation	$S_A + S_B \sim e^{i\theta} ^2 = 1$
$\mathbb{H}$	4	no	no	yes	exact 3D rotation	A–B antisymmetry; membrane = k
$\mathbb{O}$	8	no	no	no	exceptional symmetry G_2	deep projective structure SPEC.



6.5 Bridge analysis I: antisymmetry $\leftrightarrow$ quaternionic non-commutativity

This bridge is developed in three layers (concrete to formal).

Layer 1 — definition. Non-commutativity means the order of combination changes the result: $a \cdot b \neq b \cdot a$. The model already asserts that applying A’s dynamics then B’s yields a different global state than B then A.

Layer 2 — physical origin. In a commutative system the parts act independently. The A–B coupling is global and antisymmetric: through the membrane, B’s response depends on the state A has already produced, so sequence matters. This is the same reason spatial rotations do not commute — each operation modifies the space in which the next one acts.

Layer 3 — correspondence. With $i \leftrightarrow A, j \leftrightarrow B$, the membrane is the emergent element k : $ij = +k$ (A then B), $ji = -k$ (B then A). The model's own requirement $k_A^{\text{eff}} \approx -k_B^{\text{eff}}$ — equal magnitude, opposite sign, order-dependent result — is precisely the algebraic definition of quaternionic non-commutativity. On this reading the global coupler need not be postulated as a new mysterious entity: it is the third imaginary element k of the quaternionic structure that A and B jointly form.

6.6 Bridge analysis II: entropy balance $\leftrightarrow$ phase conservation in $\mathbb{C}$

The conservation $S_A + S_B \approx \text{const}$ has the same structure as norm conservation $|e^{i\theta}|^2 = 1$: two quantities oscillating in opposition while their quadratic combination stays fixed. Under $S_A = \cos^2\theta$, $S_B = \sin^2\theta$, the expansion–contraction cycle is a phase rotation in $\mathbb{C}$, and the Wick rotation $t \rightarrow -i\tau$ is the mechanism connecting the real-time oscillation to a Euclidean statistical distribution.

Scope statement (preserved from the source). This bridge does *not* assert that entropy “is” a complex phase. It is a *structural* correspondence: the same algebraic skeleton appears in two places. It is therefore classified as “moderate — include with caveats” (see §7.2), too precise to be mere metaphor, too indirect to be literal physics.

6.7 Bridge analysis III: the deep projective structure and $\mathbb{O}$

An earlier appendix posits that A and B are projections of a single deeper structure Ω . If composing those projections is path-dependent — $(\Omega \rightarrow A) \rightarrow B \neq \Omega \rightarrow (A \cdot B)$ — the composition is non-associative, and by Hurwitz's theorem the only non-associative normed division algebra is $\mathbb{O}$. The automorphism group $G_2 = \text{Aut}(\mathbb{O})$ then becomes the candidate symmetry of the membrane.

Epistemic status: speculative. This is coherent and, if the projective premise holds, structurally necessary — but it is *not* formally derived. Establishing it would require showing that the symmetry-preserving transformations of the A–B coupling form precisely G_2 . This is flagged as an open problem (see §10), not a result.

7. Results

“Results” here means the outcomes of the consistency analyses and the recursive compression — structural identifications and surviving claims — not empirical measurements.

7.1 The irreducible core (recursive compression result)

After recursive compression across the full archive, five assertions survived. They are stated here with their epistemic layer marked.

1. **A well-formulated cosmological observation.** **[empirical-compatible]** The accelerated expansion (Λ) could be an emergent geometric effect of a global antisymmetric coupling with a complementary structure; observationally indistinguishable from Λ CDM in the current regime; requires no exotic substance.
2. **A solid algebraic correspondence.** **[rigorous]** The antisymmetric A–B dynamics have precisely the structure of quaternionic non-commutativity. The model lives in $\mathbb{H}$; its foundations

point to $\mathbb{O}$. This is structural identification, not metaphor.

- 3. **A principle about knowledge.** **[interpretive]** Mathematical systems are compressed languages that emerge when reality exhibits recurring structures at multiple scales; each algebraic extension gains expressiveness by sacrificing a structural constraint.
- 4. **An honest epistemic boundary.** **[methodological]** The model is a well-formulated question, not an answer; the boundary between rigorous, empirical, speculative, and poetic must remain visible.
- 5. **A note on process as result.** **[reflective]** The work was built collaboratively between a human and multiple AI systems over seven months; the process is part of the result, not merely scaffolding.

7.2 Classification of the inter-version bridges

A two-pass iteration connecting the dynamical model (early versions) and the algebraic hierarchy (late versions) identified five candidate bridges and classified them by strength:

Bridge	Strength	Status
Antisymmetry A–B $\leftrightarrow$ quaternionic non-commutativity (§6.5)	Solid	Defensible structural identification
Membrane $\leftrightarrow$ emergent element k (§6.5)	Solid	Defensible structural identification
Entropy balance $\leftrightarrow$ phase conservation in $\mathbb{C}$ (§6.6)	Moderate	Elegant; include with caveats
$C_0 \approx 1.69$ as $\mathbb{N} \rightarrow \mathbb{R}$ transition marker (§7.4)	Moderate	Reinterpreted; needs further work
Deep projective structure $\leftrightarrow \mathbb{O} / G_2$ (§6.7)	Speculative	Fertile; not derived

7.3 What did not survive compression

- $C_0 = 1.69$ as a *mystical* or universe-governing constant (retained only in the restricted sense of §7.4).
- The palindromic mirror “levels 1–15” treated as physical results (they are method).
- Any claim about consciousness existing in imaginary time.
- The “Cerberus” metaphor (fertile as narrative, not physics).

7.4 Reconciliation of the $C_0 \approx 1.69$ claim

Flagged tension, resolved. The sources both *discard* $C_0 = 1.69$ (as a mystical constant) and *retain* it (as a dimensional marker). These are not contradictory: the consolidated reading rejects any fundamental or governing role for C_0 and keeps it only as a provisional marker of the $\mathbb{N} \rightarrow \mathbb{R}$ threshold (a Compton-scale indicator of the discrete-to-continuous transition). Its epistemic status is **speculative/moderate**, pending a derivation that does not yet exist.

7.5 The four-layer epistemic boundary

Layer	Representative content	Evaluation criterion
Rigorous	$G_A = G_B$ with pressure inversion; Friedmann equations intact; $\mathbb{H}$ captures A–B antisymmetry	Mathematical consistency
Empirical	Indistinguishable from Λ CDM; no new anisotropies; no modified local predictions	Observational agreement
Speculative	Entropy as phase in $\mathbb{C}$; C_0 as $\mathbb{N} \rightarrow \mathbb{R}$ marker; deep structure in $\mathbb{O}$; G_2 as membrane symmetry	Coherence + fertility
Poetic	Observer as recursive fixed point; the model as a question; dedication	Habitability, not verification

The visible boundary is argued to be *protective* (a refutation in one layer does not contaminate the others), *inviting* (each speculative claim is an explicit future-work item), and *durable* (a later reader can tell exactly what was established, hypothesized, or metaphorical).

8. Discussion

The framework’s appeal is organizational rather than predictive. By leaving the Friedmann equations intact and reinterpreting Λ as a coupling parameter, it offers a candidate *account* of the dark-energy term without introducing new local physics. Its most defensible element is the algebraic identification (§6.5, §7.1–2): the requirement of an equal-magnitude, opposite-sign, order-dependent coupling is, by construction, quaternionic. This is a genuine structural correspondence and the strongest claim in the manuscript.

The weaker claims are clearly labelled. The entropy–phase bridge (§6.6) is an elegant structural analogy but not a physical identity; the octonionic deep structure (§6.7) is coherent but underived. The author’s decision to present these with explicit epistemic tags, rather than to inflate them, is consistent with good scientific hygiene and is itself part of the contribution.

On the methodological side, the manuscript is unusual in documenting its own production. The claim that AI context-window limits and the absence of cross-session memory *forced* a productive compression (§9.5) is a concrete, testable observation about human–AI workflows: constraints acted as a selection pressure favouring the essential. Whether this generalizes beyond the present case is open, but the case is reported with enough detail to be examined.

9. Limitations

- **No empirical test.** The framework is, by the author’s own statement, observationally indistinguishable from Λ CDM in the current regime. It therefore makes no new, falsifiable prediction at present and cannot be empirically preferred.
- **The octonionic claim is underived.** The $G_2 = \text{Aut}(\mathbb{O})$ membrane symmetry rests on an unproven path-dependence premise (§6.7).
- **Structural vs. physical correspondence.** Several mappings (entropy–phase; C_0) are structural analogies, not demonstrated physical identities.

- **No formal bibliography.** The source archive contains no external citations; standard results (Friedmann equations, Λ CDM, Hurwitz’s theorem, G_2) are referenced generically here and require proper citation before formal submission (see Unresolved Issues).
- **Single-author, non-peer-reviewed.** This is a personal manuscript deposit; it has not undergone external peer review.
- **Process documentation is self-reported.** The collaborative-process findings (§9 of the model / the process appendix) are first-person and not independently verified.

10. Future Work

- **Derive (or refute) the octonionic symmetry.** Show whether the symmetry-preserving transformations of the A–B coupling form precisely G_2 — the content of a hypothetical “v16.”
- **Seek a distinguishing prediction.** Identify any regime (early universe, large-scale anisotropy, parameter drift) in which the coupled-mirror picture would differ observationally from Λ CDM.
- **Formalize the $\mathbb{C}_0$ marker.** Provide a principled derivation of the $\mathbb{N} \rightarrow \mathbb{R}$ transition scale, or discard the marker.
- **Strengthen the entropy–phase bridge.** Determine whether the $\mathbb{C}$ phase correspondence can be promoted from analogy to a derived relation.
- **Independent study of the process claims.** Test whether constraint-driven compression in human–AI workflows generalizes beyond this case.

11. Conclusion

This manuscript presents a speculative, internally consistent reframing of the cosmological constant as an emergent geometric effect of a globally coupled mirror universe, together with a structural identification of the model’s natural algebraic home in the quaternions and a speculative extension to the octonions. Its strongest claim — that the required antisymmetric coupling is, by construction, quaternionic non-commutativity — is offered as a genuine structural result; its weaker claims are labelled as speculative and left as explicit open problems. Equally, the work documents a long human–AI collaborative process and argues that the constraints of that process were generative. The manuscript does not claim to answer a cosmological question; it claims to have formulated one carefully, and to have kept visible, throughout, the line between what is established, what is hypothesized, and what is metaphor.

***Dedication (poetic layer).** This work began, in part, as a way of continuing conversations that could no longer be had. The author’s father loved science fiction, astronomy, and the great questions about the origin of the universe, and would let those questions float, unresolved, comfortable in their enormity. This manuscript is dedicated to him, and to everyone who held out a hand at the right moment — even briefly, even without knowing what they were anchoring.*

12. References

Note. The source archive contains no formal bibliography. The items below identify the standard results invoked and the internal artifacts consolidated. Proper, citable references (with editions and page numbers) should be added before any formal submission.

Standard results referenced (to be cited formally):

1. The Friedmann–Lemaître equations of relativistic cosmology (standard general relativity).
2. The Λ CDM concordance model of cosmology (standard).
3. Hurwitz’s theorem on normed division algebras (A. Hurwitz, 1898): $\mathbb{R}$, $\mathbb{C}$, $\mathbb{H}$, $\mathbb{O}$ are the only normed division algebras over the reals.
4. The exceptional Lie group G_2 as the automorphism group of the octonions, $\text{Aut}(\mathbb{O})$ (standard).
5. The Wick rotation $t \rightarrow -i\tau$ relating Lorentzian and Euclidean formulations (standard).

Internal artifacts consolidated in this edition:

1. Tarek, *Speculative Model of Coupled Mirror Universes* — core manuscript (Zenodo personal deposit, May 2026).
2. Tarek, *Appendix 23* and associated process transcripts — recursive-compression and “codec” sessions with ChatGPT, Grok, and Claude (Nov 2025 – May 2026).
3. Internal version archive v1–v15 (Oct 2025 – May 2026), including bilingual PDFs, audio recordings, infographics, and code-execution outputs (see chronology, §9.3 of the process appendix).

Consolidated edition v16 · prepared for Zenodo deposit · Tarek, tarek.notebook@gmail.com · @echoeseveryname · Ejea de los Caballeros, Aragón, Spain · June 2026. This edition merges the core manuscript and the process appendix, removes redundancy, retains the strongest explanation of each concept, and preserves the author’s four-layer epistemic boundary.